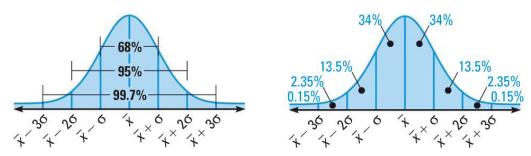
AP Statistics	Name:	
Mr Murphy	Date:	
Empirical Rule, Percentiles, and Z Scores Worksheet	Period:	

## The Empirical Rule

A lot of large data samples can be referred to as being normally distributed. When data is normally distributed, it has certain characteristics:

- 1. The mean, median, and the mode are all equivalent.
- 2. The data fits a bell shaped curve (normal curve).
- 3. About 68% of the data falls within 1 standard deviation from the mean.
- 4. About 95% of the data falls within 2 standard deviation from the mean.
- 5. About 99.7% of the data falls within 3 standard deviation from the mean.



- A machine fills 12 ounce Potato Chip bags. It places chips in the bags. Not all bags weigh exactly 12 ounces. The weight of the chips placed is normally distributed with a mean of 12.4 ounces and with a standard deviation of 0.2 ounces. The company has asked you to determine the following probabilities to aid in consumer relations concerning the weight of the bags purchased.
  - (a) If you purchase a bag filled by this dispenser what is the likelihood it has less than 12 ounces?
  - (b) If you purchase a bag filled by this dispenser what is the likelihood it has less than 12.6 ounces?
  - (c) If you purchase a bag filled by this dispenser what is the likelihood it has between 12 and 12.6 ounces?

**Percentiles -** A percentile is a measure that tells us what percent of the total (relative) frequency scored at or below that measure

(d) What weight of the bag is represented by the 84th percentile?

## z-scores

- tell us how many standard deviations a term is above or below the mean
- use z-scores to normalize data

$$z = \frac{x - \mu}{\sigma}$$

2. If we have a normally distributed data set where  $\mu = 8$  and  $\sigma = 2$ , find the *z*-score for the following data points.

(a) x = 12

(b) x = 7

Conc	lusion	about	z-scores
	IUSIUII	about	Z-360163

z-scores have a \_\_\_\_\_\_ value if the element lies above the mean.
z-scores have a \_\_\_\_\_ value if the element lies below the mean.

- 3. Women's heights are normally distributed with a mean of 63.6 inches and a standard deviation of 2.5 inches. Jodi is 61.1 inches tall.
  - (a) What is the difference between Jodi's height and the mean?
  - (b) How many standard deviations is that?
  - (c) Convert Jodi's height to a z-score.
  - (d) How do your answers to (b) and (c) compare?

- 4. Heights of men are normally distributed with a mean of 69.0 inches and a standard deviation of 2.8 inches. Find each of the following *z*-scores and tell if it is unusual.
  - (a) Shaquille O'Neal is 7 ft. 1 in. tall.
  - (b) Bob Jenkins 5 ft. 4 in.
  - (c) Textbook's author 69.72 inches tall.



Why do we find the z-score? .... A way to compare apples and oranges!



- 5. The average apple has a diameter of 3.25 inches with a standard deviation of 0.5 inch. The average orange has a diameter of 4.5 inches and has a standard deviation of 1 inch. If I have an apple with a diameter of 4 inches and an orange with a diameter of 5.5 inches, which fruit is largest compared to others of its kind?
- 6. Inside what interval does the corresponding z-score for the 30th percentile fall?
  - (a) -2 < z < -1
  - (b) -1 < z < 0
  - (c) 0 < z < 1
  - (d) 1 < z < 2
  - (e) 2 < x < 3

## Checkpoint

- 1. A study of elite distance runners found a mean body weight of 63.1 kilograms (kg), with a standard deviation of 4.8 kg. Assume a normal distribution.
  - (a) Use the Empirical Rule to find intervals centered at the mean that will include 68%, 95%, and 99.7% of the weights of the runners. Draw the normal curve to the right.



- 68%: \_\_\_\_\_
- 95%: \_\_\_\_\_
- 99.7%:
- (b) What weight would represent the 84th percentile?
- (c) A weight in what range would represent the bottom 16% of the weights?
- (d) What percent of weights are higher than 77.5kg?
- (e) The 80th percentile would be between what two weights?

2.	Batteries of 2 brands are compared. Brand A has a mean life of 48 months and a standard deviation of 2 months. Brand B has a mean of 48 months and a standard deviation of 6 months. Which brand would you say is the better choice? Why?
3.	Test 1 has a mean of 128 and $s=34$ . Test 2 has a mean of 86 and $s=18$ . Test 3 has a mean of 15 and $s=5$ . Which of these scores is the highest relative score? Test 1 score of 144 or Test 2 score of 90 or Test 3 score of 18.
4.	To the nearest whole number, what percentile is associated with a $z$ -score of $z$ = -0.68?
	<ul> <li>(a) 10th percentile</li> <li>(b) 40th percentile</li> <li>(c) 50th percentile</li> <li>(d) 25th percentile</li> <li>(e) 75th percentile</li> </ul>
5.	If the range of a normally distributed data set is 25, what's a reasonable estimate for the standard deviation?
	(a) 1 (b) 2.5 (c) 5 (d) 10 (e) 15
6.	SAT scores of females have a normal distribution with a mean of 998 and $s=202$ . A college has a minimum of 900 as one of its requirements for admission. About what percentage of females do NOT satisfy this requirement?