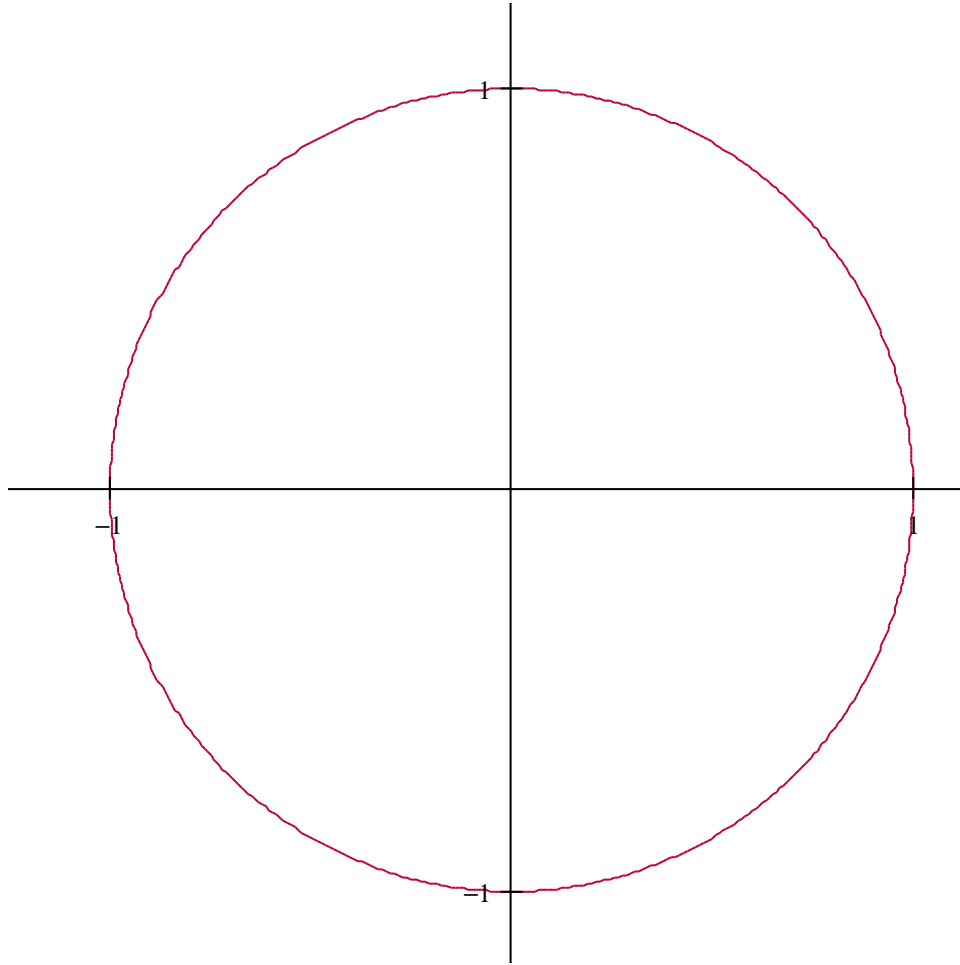
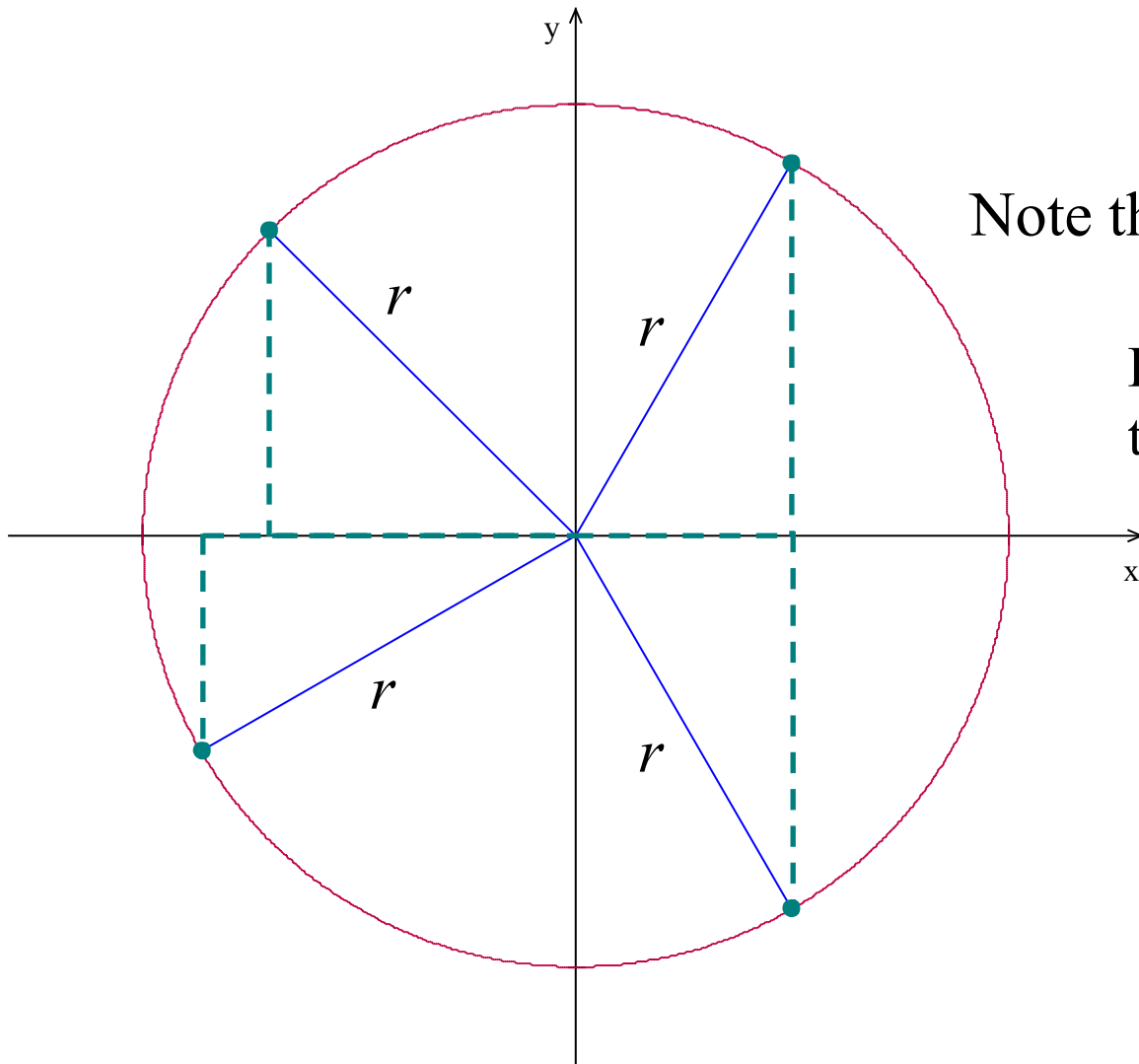


A Circle of radius 1



$$x^2 + y^2 = 1$$

# A Circle



$$x^2 + y^2 = r^2$$

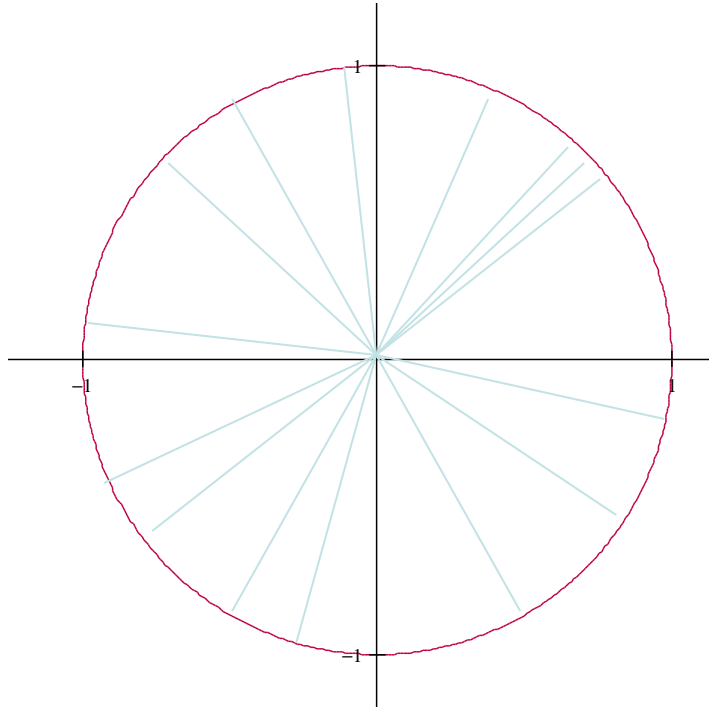
Note the Pythagorean form

How does the Pythagorean theorem apply here?

The  $x$  and  $y$  coordinates are also side lengths of a right triangle with the radius as the hypotenuse

Regardless of the quadrant in which the points lie

## A Circle



$$x^2 + y^2 = 1$$

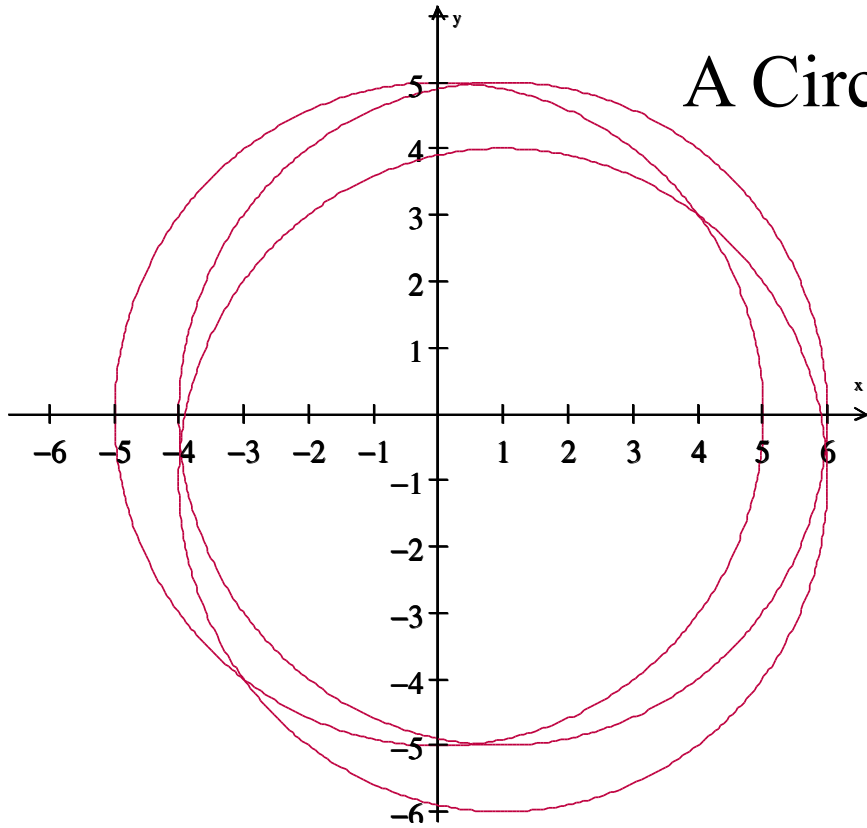
Note the Pythagorean form

Notice also that each point on the circle is equidistant from the center

What if we altered the coefficients of the equation?

$$x^2 + y^2 = 25$$

## A Circle



$$x^2 + y^2 = 25$$

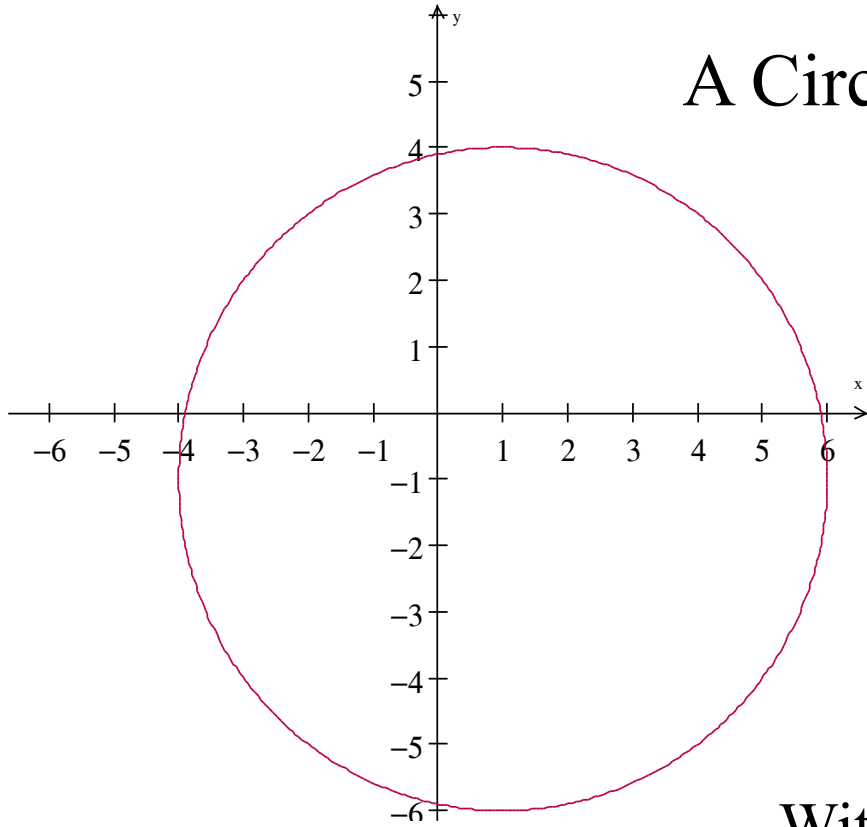
So now our radius is 5

Remembering parabolas,  
what could I do to this  
equation to move the center 1  
to the right?

$$(x - 1)^2 + (y + 1)^2 = 25$$

How about 1 down?

## A Circle



$$x^2 + y^2 = 25$$

So the general equation for a circle is:

$$(x - h)^2 + (y - k)^2 = r^2$$

With center  $(h, k)$  and radius  $r$

What if your equation looked like this:  $x^2 - 2x + y^2 + 2y - 23 = 0$

Hint: Try completing the squares

$$(x - 1)^2 + (y + 1)^2 = 25 \quad \text{How?}$$

# A Circle

So the general equation for a circle is:

$$(x-h)^2 + (y-k)^2 = r^2$$

With center  $(h, k)$  and radius  $r$

What if your equation looked like this:  $x^2 - 2x + y^2 + 2y - 23 = 0$

$$(x^2 - 2x + 1) + (y^2 + 2y + 1) = 23 + 1 + 1$$

Add 1 to complete  
each square

Add the same  
numbers to the other  
side

$$(x-1)^2 + (y+1)^2 = 25$$