Recall from last unit:

Sampling Distributions for Sample Proportions

• The mean of the sampling distribution is the same as the proportion of the population:

$$\mu_{\hat{p}} = p$$

• The **standard deviation** of the sampling distribution gets smaller according to this equation:

$$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$$

Notice how with proportions, we calculate our own SD from the info given

- We assume **Normality** through three checkpoints:
 - 1. $np \ge 10$
 - $2. n(1-p) \ge 10$
 - 3. Assuming that the sample size is less than 10% of the population
- Calculate **probabilities** using *normalcdf*

Sampling Distributions for **Differences** in Sample Proportions

• The **mean** of the sampling distribution is the same as the proportion of the population:

$$\mu_{\hat{p}_1 - \hat{p}_2} = p_1 - p_2$$

• The standard deviation of the sampling distribution gets smaller according to this equation:

$$\boldsymbol{\sigma}_{\hat{p}_1 - \hat{p}_2} = \sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}$$

• We assume **Normality** through the same checkpoints but for both proportions:

$$n_1 p_1 \ge 10 \qquad n_2 p_2 \ge 10 \\ n_1 (1 - p_1) \ge 10 \qquad n_2 (1 - p_2) \ge 10$$

Assume that the samples are both independent and less than 10% of each population

• Calculate **probabilities** using *normalcdf*

Are each proportions large enough for their sample sizes to be large enough to meet sample proportion assumptions?

| $n_M p_M \ge 10$ | $n_B p_B \ge 10$ |
|------------------|------------------|
| $20p_M \ge 10$ | $10p_B \ge 10$ |
| $p_M \ge 0.5$ | $p_B \ge 1$ |

 $p_M = 0.48$

Looks like the sample size is too small especially in the case of Bay's numbers

Since they both know that they should do a little more research to be sure now, they agree to sample 40 days for both Bay and Madison.

Find the mean and standard deviation of the difference of their sample proportions

$$40(0.48) = 19.2 \ge 10 \qquad \qquad \mu_{\hat{p}_M - \hat{p}_B} = 0.48 - 0.34 = .14$$

$$40(.34) = 13.6 \ge 10$$

The sample size is less than 10% of the population

They've both been playing Farm Story for at least two years which is longer than 400 days

$$\sigma_{\hat{p}_M - \hat{p}_B} = \sqrt{\frac{p_M(1 - p_M)}{n_M} + \frac{p_B(1 - p_B)}{n_B}}$$
$$= \sqrt{\frac{0.48(1 - 0.48)}{40} + \frac{0.34(1 - 0.34)}{40}}$$

= 0.1089

Madison, who wants Lola and Sam to understand her dedication to her game, is certain that less than 10% of the time, her Farm Story time will be less than Bay's. Is she right?

So we are looking for where the distribution is less than 0

 $P(\hat{p}_M - \hat{p}_B < 0)$

normalcdf(-1E99, 0, 0.14, 0.1089)

0.0992 or 9.92%

Looks like Madison is right...by the tiniest of margins



Since they both know that they should do a little more research to be sure now, they agree to sample 40 days for both Bay and Madison.

You may have noticed that this doesn't seem very practical especially if we already know the actual proportions. Most of the time in real life we won't have much actual population data. That's why we sample in the first place. The main purpose of these problems is to practice working with the formulas before we start working with populations with unknown parameters