# Probability Spaces and <br> Tree Diagrams 

The data table below gives data for 103,870 women on their current and past marital status.

If one of these women were chosen at random, the probability of finding a married woman between the ages of 18 and 29 is...
$\mathrm{P}(18-29 \&$ Married $)=7,842 / 103,870 \approx .0755$

Age and marital status of women in the U. S. (thousands)

|  | Age |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
|  | $\mathbf{1 8 - 2 9}$ | $\mathbf{3 0 - 6 4}$ | 65 and over | Total |
| Married | 7,842 | 43,808 | 8,270 | 59,920 |
| Never Married | 13,930 | 7,184 | 751 | 21,865 |
| Widowed | 36 | 2,523 | 8,385 | 10,944 |
| Divorced | 704 | 9,174 | 1,263 | 11,141 |
| Total | 22,512 | 62,689 | 18,669 | 103,870 |

Source: Data for 1999 from the 2000 Statistical Abstract of the U.S.
$\mathrm{P}($ Widow who is 65 and over $)=\mathbf{8 , 3 8 5} / \mathbf{1 0 3}, \mathbf{8 7 0}=0.081$
$\mathrm{P}($ Married $)=\mathbf{5 9 , 9 2 0} / \mathbf{1 0 3}, 870=0.577$
$\mathrm{P}(30-64$ years old $)=\mathbf{6 2 , 6 8 9} / \mathbf{1 0 3}, 870=0.604$
$\mathrm{P}($ Divorced or 18-29) $=32,949 / 103,870$ ???
$\mathrm{P}($ Never married or 65 and over $)=$
Age and marital status of women in the U. S. (thousands)

|  | Age |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
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$\mathrm{P}($ Divorced or $18-29)=32,949 / 103,870$ ???
$\mathrm{P}($ Never married or 65 and over $)=39,783 / 103,870$

21,865
$+18,669$

| $-\quad 751$ |
| :--- |

39,783

751 is contained in both 18,669 and 21,865 so we have to subtract one

Age and marital status of women in the U. S. (thousands)

|  | Age |  |  | Total |
| :---: | :---: | :---: | :---: | :---: |
|  | 18-29 | 30-64 | 65 and over |  |
| Married | 7,842 | 43,808 | 8,270 | 59,920 |
| Never Married | 13,930 | 7,184 | 751 | 21,865 |
| Widowed | 36 | 2,523 | 8,385 | 10,944 |
| Divorced | 704 | 9,174 | 1,263 | 11,141 |
| Total | 22,512 | 62,689 | 18,669 | 103,870 |

Source: Data for 1999 from the 2000 Statistical Abstract of the U.S.

Suppose you are choosing at random from only the married women
$\mathrm{P}($ Age 30-64 | Married Women $)=43,808 / 59,920$

This symbol represents conditional probability...to be continued

Age and marital status of women in the U. S. (thousands)

|  | Age |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
|  | $\mathbf{1 8 - 2 9}$ |  |  | $\mathbf{3 0 - 6 4}$ |
| $\mathbf{6 5}$ and over | Total |  |  |  |
| Married | 7,842 | 43,808 | 8,270 | 59,920 |
| Never Married | 13,930 | 7,184 | 751 | 21,865 |
| Widowed | 36 | 2,523 | 8,385 | 10,944 |
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Source: Data for 1999 from the 2000 Statistical Abstract of the U.S.

Now let's revisit the one and one situation: A player with a free throw percentage of $60 \%$ goes to the line for a one and one. If he/she makes the first shot, he/she gets a second. If he/she misses the first shot, the ball is live. What is the most likely outcome: Zero, One point, or Two points.

To do this, make a tree diagram:

First Shot


$\mathrm{P}($ Zero $)=0.4$

Second Shot
We expect that the player will make two shots $60 \%$ of the $60 \%$ of the time that he/she makes the first shot
$P($ Makes it $)=0.6$
$\mathrm{P}($ Two points $)=0.36$

$$
\mathrm{P}(\text { misses })=0.4
$$

Meaning that we need to multiply the two probabilities
$\mathrm{P}($ One Point $)=0.24$

