Probability Spaces and Tree Diagrams

The data table below gives data for 103,870 women on their current and past marital status.

If one of these women were chosen at random, the probability of finding a married woman between the ages of 18 and 29 is...

 $P(18-29 \& Married) = 7,842/103,870 \approx .0755$

		Age		
	18-29	30-64	65 and over	Total
Married	7,842	43,808	8,270	59,920
Never Married	13,930	7,184	751	21,865
Widowed	36	2,523	8,385	10,944
Divorced	704	9,174	1,263	11,141
Total	22,512	62,689	18,669	103,870

Age and marital status of women in the U.S. (thousands)

P(Widow who is 65 and over) = 8,385/103,870 = 0.081

P(Married) = **59,920/103,870** = 0.577

P(30-64 years old) = 62,689/103,870 = 0.604

P(Divorced or | 18-29) = 32,949/103,870 ???

 $\begin{array}{r}
11,141 \\
+ 22,512 \\
- 704 \\
\hline
32,949
\end{array}$

704 is contained in both 11,141 and 22,512 so we have to subtract one

P(Never married or 65 and over) =

Age and marital status of women in the U.S. (thousands)

		Age		
	18-29	30-64	65 and over	Total
Married	7,842	43,808	8,270	59,920
Never Married	13,930	7,184	751	21,865
Widowed	36	2,523	8,385	10,944
Divorced	704	9,174	1,263	11,141
Total	22,512	62,689	18,669	103,870

P(Widow who is 65 and over) = 8,385/103,870 = 0.081

P(Married) = **59,920/103,870** = 0.577

P(30-64 years old) = 62,689/103,870 = 0.604

P(Divorced or 18-29) = 32,949/103,870 ???

21,865 + 18,669 - 751 39,783

751 is contained in both18,669 and 21,865 so wehave to subtract one

P(Never married or 65 and over) = 39,783/103,870

Age and marital status of women in the U.S. (thousands)

		Age		
	18-29	30-64	65 and over	Total
Married	7,842	43,808	8,270	59,920
Never Married	13,930	7,184	751	21,865
Widowed	36	2,523	8,385	10,944
Divorced	704	9,174	1,263	11,141
Total	22,512	62,689	18,669	103,870

Suppose you are choosing at random from only the married women

P(Age 30-64 | Married Women) = 43,808/59,920

This symbol represents *conditional probability*...to be continued

		Age		
	18-29	30-64	65 and over	Total
Married	7,842	43,808	8,270	59,920
Never Married	13,930	7,184	751	21,865
Widowed	36	2,523	8,385	10,944
Divorced	704	9,174	1,263	11,141
Total	22,512	62,689	18,669	103,870

Age and marital status of women in the U.S. (thousands)

Now let's revisit the one and one situation: A player with a free throw percentage of 60% goes to the line for a one and one. If he/she makes the first shot, he/she gets a second. If he/she misses the first shot, the ball is live. What is the most likely outcome: Zero, One point, or Two points.

To do this, make a tree diagram:

P(Makes it) =
$$0.6$$
P(misses) = 0.4 First Shot $P(Zero) = 0.4$ Second Shot $P(Makes it) = 0.6$ We expect that the player
will make two shots 60% of
the 60% of the time that
he/she makes the first shot $P(Makes it) = 0.6$ P(Makes it) = 0.6 $P(misses) = 0.4$ We expect that the player
will make two shots 60% of
the 60% of the time that
he/she makes the first shot $P(Two points) = 0.36$ P(One Point) = 0.24